## Relational Algebra

Relational algebra is a procedural query language. It gives a step by step process to obtain the result of the query. It uses operators to perform queries.

Types of Relational operation


1. Select Operation:
o The select operation selects tuples that satisfy a given predicate.
o lt is denoted by sigma ( $\sigma$ ).
2. Notation: $\sigma \mathrm{p}(\mathrm{r})$

## Where:

$\boldsymbol{\sigma}$ is used for selection prediction $\boldsymbol{r}$ is used for relation $\mathbf{p}$ is used as a propositional logic formula which may use connectors like: AND OR and NOT. These relational can use as relational operators like $=, \neq, \geq,<,>, \leq$.

## For example: LOAN Relation

| BRANCH_NAME | LOAN_NO | AMOUNT |
| :--- | :--- | :--- |
| Downtown | L-17 | 1000 |
| Redwood | L-23 | 2000 |
| Perryride | $\mathrm{L}-15$ | 1500 |
| Downtown | $\mathrm{L}-14$ | 1500 |
| Mianus | $\mathrm{L}-13$ | 500 |
| Roundhill | $\mathrm{L}-11$ | 900 |
| Perryride | $\mathrm{L}-16$ | 1300 |

INPUT:
o BRANCH_NAME="perryride" (LOAN)

Output:

BRANCH NAME
Perryride
Perryride

LOAN NO
L-15
L-16

AMOUNT
1500
1300

## 2. Project Operation:

This operation shows the list of those attributes that we wish to appear in the result. Rest of the attributes are eliminated from the table.

It is denoted by $П$.

Notation: П A1, A2, An (r)
Where
$A 1, A 2, A 3$ is used as an attribute name of relation $r$.

Example: CUSTOMER RELATION

NAME

Jones
Smith
Hays
Curry
Johnson
Brooks

STREET

Main
North
Main
North
Alma
Senator

CITY

Harrison
Rye
Harrison
Rye
Brooklyn
Brooklyn

## Input:

$\Pi$ NAME, CITY (CUSTOMER)

## Output:

NAME

Johns
Smith
Hays
Curry
Johnson
Brooks

CITY

Harrison
Rye
Harrison
Rye
Brooklyn
Brooklyn

## 3. Union Operation:

Suppose there are two tuples $R$ and $S$. The union operation contains all the tuples that are either in R or $S$ or both in $R \& S$.

It eliminates the duplicate tuples. It is denoted by $U$.

Notation: R U S

A union operation must hold the following condition:
$R$ and $S$ must have the attribute of the same number.

Duplicate tuples are eliminated automatically.

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Example:
DEPOSITOR RELATION
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## CUSTOMER NAME

Johnson A-101
Smith
Mayes
Turner
Johnson
Jones
Lindsay

## BORROW RELATION

## CUSTOMER_NAME

Jones
Smith
Hayes
Jackson
Curry
Smith
Williams
Input:

## Output:

## CUSTOMER NAME

Johnson
Smith

Hayes
Turner
Jones
Lindsay
Jackson
Curry
Williams
Mayes
4. Set Intersection:

Suppose there are two tuples $R$ and $S$. The set intersection operation contains all tuples that are in both $R \& S$.

It is denoted by intersection $\cap$.

Notation: $\mathrm{R} \cap \mathrm{S}$
Example: Using the above DEPOSITOR table and BORROW table INPUT:

П CUSTOMER_NAME (BORROW) $\cap$ П CUSTOMER_NAME (DEPOSITOR)

## OUTPUT:

## CUSTOMER NAME

Smith
Jones

## 5. Set Difference:

Suppose there are two tuples R and S. The set intersection operation contains all tuples that are in R but not in S .

It is denoted by intersection minus (-).

Notation: R - S

Example: Using the above DEPOSITOR table and BORROW table Input:

## П CUSTOMER_NAME (BORROW) - П CUSTOMER_NAME (DEPOSITOR)

## Output:

## CUSTOMER NAME

Jackson

Hayes
Williams
Curry

## 6. Cartesian Product:

The Cartesian product is used to combine each row in one table with each row in the other table. It is also known as a cross product.

It is denoted by X .

Notation: E X D

Example:

## EMPLOYEE

EMP_ID

1
2

EMP_NAME

Smith
Harry

EMP_DEPT

A
C

## DEPARTMENT

DEPT_NO DEPT_NAME

A
B
C

Input:

EMPLOYEE X DEPARTMENT

Marketing Sales
Legal

## Output:

| EMP_ID | EMP_NAME | EMP_DEPT | DEPT_NO | DEPT_NAME |
| :--- | :--- | :--- | :--- | :--- |
| 1 | Smith | A | A | Marketing |
| 1 | Smith | A | B | Sales |
| 1 | Smith | A | C | Legal |
| 2 | Harry | C | A | Marketing |

7. Rename Operation:

The rename operation is used to rename the output relation. It is denoted by rho ( $\rho$ ).

Example: We can use the rename operator to rename STUDENT relation to STUDENT1.
$\rho(S T U D E N T 1$, STUDENT)

Note:Apart from these common operations Relational algebra can be used in Join operations.

## Relational Calculus

Relational calculus is a non-procedural query language. In the non-procedural query language, the user is concerned with the details of how to obtain the end results.

- The relational calculus tells what to do but never explains how to do.


## Types of Relational calculus:



## 1. Tuple Relational Calculus (TRC)

- The tuple relational calculus is specified to select the tuples in a relation. In TRC, filtering variable uses the tuples of a relation.
o The result of the relation can have one or more tuples.


## Notation:

$\{T \mid P(T)\}$ or $\{T \mid$ Condition ( T$)\}$
Where

## $T$ is the resulting tuples

$\mathbf{P}(\mathbf{T})$ is the condition used to fetch $T$.

## For example:

\{ T.name | Author(T) AND T.article = 'database' \}
OUTPUT: This query selects the tuples from the AUTHOR relation. It returns a tuple with 'name' from Author who has written an article on 'database'. TRC (tuple relation calculus) can be quantified. In TRC, we can use Existential ( $\exists$ ) and Universal Quantifiers ( $\forall$ ).

## For example:

$\{R \mid \exists T \in$ Authors(T.article='database' AND R.name=T.name) $\}$
Output: This query will yield the same result as the previous one.

## 2. Domain Relational Calculus (DRC)

- The second form of relation is known as Domain relational calculus. In domain relational calculus, filtering variable uses the domain of attributes.
- Domain relational calculus uses the same operators as tuple calculus. It uses logical connectives $\wedge$ (and), $\vee$ (or) and $\urcorner$ (not).
- It uses Existential ( $\exists$ ) and Universal Quantifiers ( $\forall$ ) to bind the variable


## Notation:

$\{a 1, a 2, a 3, \ldots, a n \mid P(a 1, a 2, a 3, \ldots, a n)\}$

## Where

$\mathbf{a 1}, \mathbf{a 2}$ are attributes $\mathbf{P}$ stands for formula built by inner attributes

## For example:

\{< article, page, subject $>\mid \in$ javatpoint $\wedge$ subject = 'database' $\}$

Output: This query will yield the article, page, and subject from the relational javatpoint, where the subject is a database.

